

# Physics of Stars and Measurement Data: Part I

**Boris V.Vasiliev**

Independent Researcher, Russia

\*Corresponding Author: bv.vasiliev@narod.ru

Copyright ©2014 Horizon Research Publishing All rights reserved.

**Abstract** The explanation of dependencies of the parameters of the stars and the Sun which was measured by astronomers is considered as a main task of the physics of stars. This theory is based on taking into account of the existence of a gravity-induced electric polarization of intra-stellar plasma because this plasma is an electrically polarized substance. The accounting of the gravity-induced electric polarization gives the explanation to data of astronomical measurements: the temperature-radius-mass-luminosity relations, the spectra of seismic oscillations of the Sun, distribution of stars on their masses, magnetic fields of stars and etc. The stellar radiuses, masses and temperatures are expressed by the corresponding ratios of the fundamental constants, and individuality of stars are determined by two parameters - by the charge and mass numbers of nuclei, from which a stellar plasma is composed. This theory is the lack of a collapse in the final stage of the star development, as well as "black holes" that could be results from a such collapse.

**Keywords** Electric Polarization, Plasma, Stellar Mass, Stellar Temperature, Stellar Radius, Seismic Oscillations, Magnetic Field

**PACS:** 64.30.+i; 95.30.-k

---

## 1 Introduction

### 1.1 Astrophysics and astronomical measurements

*"A question that sometimes  
drives me hazy:  
am I or are the others crazy?"*  
A.Einstein

It is obvious that the primary goal of modern astrophysics must be a creation of a star theory that can explain the existence of dependencies of parameters of stars and of the Sun, which are measured by astronomers.

The technical progress of astronomical measurements in the last decade has revealed the existence of different relationships that associate together the physical parameters of the stars.

To date, there are about a dozen of such new discovered relationships: it is dependencies of temperature-radius-luminosity-mass of stars, the spectra of seismic oscillations of the Sun, distribution of stars on mass, the dependence of the magnetic fields of stars from their moments and speeds of rotation, etc.

All these relationships are defined by phenomena which occurring inside stars. So the theory of the internal structure of stars should be based on these quantitative data as on boundary conditions.

Existing theories of stellar interiors can not explain of the new data. The modern astrophysics<sup>1</sup> prefers speculative considerations. It elaborates qualitative theories of stars that are not pursued to such quantitative estimates, which could be compared with the data of astronomers. Everything is done in such a way as if the new astronomical data are absent. Of course, the astrophysical community knows about the existence of dependencies of stellar parameters which were measured by astronomers. However, in modern astrophysics it is accepted to think, that if an explanation of a dependency is not found, that it can be referred to the category of empirical one and it need no an explanation. The so-called empirical relations of stellar luminosities and temperatures - the Hertzsprung-Russell diagram - is known about the hundred years but its quantitative

---

<sup>1</sup>The modern astrophysics has a whole series of different branches. It is important to stress that all of them except the physics of hot stars beyond the scope of this consideration; we shall use the term "astrophysics" here and below in its initial meaning - as the physics of stars.

explanation is not found.

The reason that prevents to explain these relationships is due to the wrong choice of the basic postulates of modern astrophysics. Despite of the fact that all modern astrophysics believe that the stars consist from a plasma, it historically turned out that the theory of stellar interiors does not take into account the electric polarization of the plasma, which must occur within stars under the influence of their gravitational field. Modern astrophysics believes that the gravity-induced electric polarization (GIEP) of stellar plasma is small and it should not be taken into account in the calculations, as this polarization was not taken into account in the calculations at an early stage of development of astrophysics, when about a plasma structure of stars was not known. However, plasma is an electrically polarized substance, and an exclusion of the GIEP effect from the calculation is unwarranted. Moreover without of the taking into account of the GIEP-effect, the equilibrium stellar matter can not be correctly founded and a theory would not be able to explain the astronomical measurements. Accounting GIEP gives the theoretical explanation for the all observed dependence.

As shown below, the account of the gravity-induced electric polarization of the intra-stellar plasma gives possibility to develop a model of the star, in which all main parameters - the mass of the star, its temperature, radius and luminosity - are expressed by certain combinations of world constants and the individuality of stars is determined by only two parameters - the mass and charge number of nuclei, from which the plasma of these stars is composed. It gives the quantitatively and fairly accurate explanation of all dependencies, which were measured by astronomers.

The important feature of this stellar theory, which is built with the GIEP accounting, is the lack of a collapse in the final stage of the star development, as well as "black holes" that could be results from a such collapse. The main features of this concept were previously published in [1]-[3].

## 1.2 The basic postulate of astrophysics

We can assume that modern astrophysics emerged in the early twentieth century and milestone of this period was the work R. Emden «Die Gaskugeln». It has laid the basis for the description of stars as gas spheres. Gases can be characterized by different dependencies of their density from pressure, ie they can be described by different polytropes. According to Emden the equations of state of the gases producing the stars determine their characteristics - it can be either a dwarf, or a giant, or main sequence star, etc. The such approach to the description of stars determined the choice of postulates needed for the theory.

Any theory based on its system of postulates.

The first basic postulate of astrophysics - the Euler equation - was formulated in a mathematical form by L.Euler in a middle of 18th century for the "terrestrial" effects description. This equation determines the equilibrium condition of liquids or gases in a gravitational field:

$$\gamma \mathbf{g} = -\nabla P. \quad (1)$$

According to it the action of a gravity forth  $\gamma \mathbf{g}$  ( $\gamma$  is density of substance,  $\mathbf{g}$  is the gravity acceleration) in equilibrium is balanced by a forth which is induced by the pressure gradient in the substance.

All modern models of stellar interior are obtained on the base of the Euler equation. These models assume that pressure inside a star monotone increases depthward from the star surface. As a star interior substance can be considered as an ideal gas which pressure is proportional to its temperature and density, all astrophysical models predict more or less monotonous increasing of temperature and density of the star substance in the direction of the center of a star.

While we are talking about materials with atomic structure, there are no doubt about the validity of this equation and its applicability. This postulate is surely established and experimentally checked by "terrestrial" physics. It is the base of an operating of series of technical devices - balloons, bathyscaphes and other.

Another prominent astrophysicist first half of the twentieth century was A. Eddington. At this time I. Langmuir discovered the new state of matter - plasma. A.Eddington was first who realized the significance of this discovery for astrophysics. He showed that the stellar matter at the typical pressures and temperatures, should be in the plasma state.

## 1.3 The another postulate

The polarizability of atomic matter is negligible. <sup>2</sup>

There was not needs to take into account an electric polarization at a consideration of cosmic bodies which are composed by atomic gases.

But plasma is an electrically polarized substance.

*It is necessary to take into account GIEP of intra-stellar plasma.*

Therefore, at consideration of an equilibrium in the plasma, the term describing its possible electrical polarization  $\mathfrak{P}$  should be saved in the Euler equation:

$$\gamma \mathbf{g} + \mathfrak{P} \nabla \mathfrak{P} + \nabla P = 0, \quad (2)$$

<sup>2</sup>If you do not take account of ferroelectrics, piezoelectrics and other similar substances. Their consideration is not acceptable here.

This leads to the possibility of the existence of a fundamentally new equilibrium state of stellar matter, at which it has a constant density and temperature:

$$\begin{aligned}\nabla P &= 0 \\ \gamma \mathbf{g} + \mathfrak{P} \nabla \mathfrak{P} &= 0,\end{aligned}\quad (3)$$

that radically distinguishes this equilibrium state from equilibrium, which is described by the Eq.(1).

### 1.3.1 Thus two postulates can be formulated. Which of these postulates is correct?

The general rule speaks for taking into account the effect of the polarization: at the beginning of determination of the equilibrium equations, one must consider all forces which, it seems, can influence it and only in the result of calculations discard small influences. However, this argument is not strong.

The method of false postulate rejecting was developed in the late Middle Ages, when this problem was sharply.<sup>3</sup> The scientific approach to choosing the right postulates was developed by Galileo.

### 1.3.2 The Galileo's method

The modern physics begins its formation at last 16 c. - middle 17 c. mainly with works of W.Gilbert and G.Galileo. They introduce into practice the main instrument of the present exact science - the empirical testing of a scientific hypothesis. Until that time false scientific statements weren't afraid of an empirical testing. A flight of fancy was dainty and refined than an ordinary and crude material world. The exact correspondence to a check experiment was not necessary for a philosophical theory, it almost discredited the theory in the experts opinion. The discrepancy of a theory and observations was not confusing at that time.

Now the empirical testing of all theoretical hypotheses gets by a generally accepted obligatory method of the exact science. As a result all basic statements of physics are sure established and based on the solid foundation of an agreement with measurement data.

To solve the problem of the correct choice of the postulate, one has the Galileo's method. It consists of 3 steps:

(1) *to postulate a hypothesis about the nature of the phenomenon, which is free from logical contradictions;*

(2) *on the base of this postulate, using the standard mathematical procedures, to conclude laws of the phenomenon;*

(3) *by means of empirical method to ensure, that the nature obeys these laws (or not) in reality, and to confirm (or not) the basic hypothesis.*

The use of this method gives a possibility to reject false postulates and theories, provided there exist a necessary observation data, of course.

Let's see what makes this method in our case.

Both postulates are logically consistent - and (1), and (2).

The theory constructed on the basis of the first postulate is all modern astrophysics. There are a lot of laws that are good mutually agreed upon.

### 1.3.3 What does the the astronomic measurement data express?

Are there actually astronomic measurement data, which can give possibility to distinguish "correct" and "incorrect" postulates of stellar interior physics? What must one do, if the direct measurement of the star interior construction is impossible?

Previously such data were absent. They appeared only in the last decade. The technical progress of astronomical measurements in the last decade discovered that the physical parameters of the stars are related together. However, these new data do not fit to models of modern astrophysics.

It seems clear to me that the primary goal of modern astrophysics is to create a theory that explains the dependencies of parameters of stars and of the Sun, which are measured by astronomers in recent decades.

## 1.4 About a star theory development

The following chapters will be devoted to the construction of the theory of stars with taking into account of the GIEP-effect (3) and comparisons of the resulting model with measurement data.

It will be shown below that all these dependencies obtain a quantitative explanation. At that all basic measuring parameters of stars - masses, radii, temperatures - can be described by definite rations of world constants, and it gives a good agreement with measurement data.

The correct choice of the substance equilibrium equation is absolute requirement of an development of the star theory which can be in agreement with measuring data.

To simplify a task of formulation of the such theory, we can accept two additional postulates.

<sup>3</sup>W. Gilbert, in his book «De magnetibus, magneticisque corporibus etc»(1600) pointed out that only experiment can prove the fallacy of a number of judgments which are generally accepted in educated society. Without experimental verification, the common judgments can be often very strange.

A hot star generates an energy into its central region continuously. At the same time this energy radiates from the star surface. This radiation is not in equilibrium relatively stellar substance. It is convenient to consider that the star is existing in its stationary state. It means that the star radiation has not any changing in the time, and at that the star must radiate from its surface as much energy as many it generates into its core. At this condition, the stellar substance is existing in stationary state and time derivatives from any thermodynamical functions which is characterizing for stellar substance are equal to zero:

$$\frac{dX}{dt} = 0. \quad (4)$$

Particularly, the time derivative of the entropy must be equal to zero in this case. I.e. conditions of an existing of each small volume of stellar substance can be considered as adiabatic one in spite of the presence of the non-equilibrium radiation. We shall use this simplification in Section VI.

The second simplification can be obtained if to suppose that a stationary star reaches the minimum of its energy after milliards years of development. (Herewith we exclude from our consideration stars with "active lifestyle". The interesting problem of the transformation of a star falls out of examination too).

The minimum condition of the star energy gives possibility to determine main parameters of equilibrium stellar substance - its density and temperature.

It is reasonable to start the development of the star theory from this point. So the problem of existing of the energy-favorable density of the stellar substance and its temperature will be considered in the first place in the next Section.

## 2 The energy-favorable state of hot dense plasma

### 2.1 The properties of a hot dense plasma

#### 2.1.1 A hot plasma and Boltzman's distribution

Free electrons being fermions obey the Fermi-Dirac statistic at low temperatures. At high temperatures, quantum distinctions in behavior of electron gas disappear and it is possible to consider electron gas as the ideal gas which obeys the Boltzmann's statistics. At high temperatures and high densities, all substances transform into electron-nuclear plasma. There are two tendencies in this case. At temperature much higher than the Fermi temperature  $T_F = \frac{\mathcal{E}_F}{k}$  (where  $\mathcal{E}_F$  is Fermi energy), the role of quantum effects is small. But their role grows with increasing of the pressure and density of an electron gas. When quantum distinctions are small, it is possible to describe the plasma electron gas as a the ideal one. The criterium of Boltzman's statistics applicability

$$T \gg \frac{\mathcal{E}_F}{k}. \quad (5)$$

hold true for a non-relativistic electron gas with density  $10^{25}$  particles in  $cm^3$  at  $T \gg 10^6 K$ .

At this temperatures, a plasma has energy

$$\mathcal{E} = \frac{3}{2}kTN \quad (6)$$

and its EOS is the ideal gas EOS:

$$P = \frac{NkT}{V} \quad (7)$$

But even at so high temperatures, an electron-nuclear plasma can be considered as ideal gas in the first approximation only. For more accurate description its properties, the specificity of the plasma particle interaction must be taken into account and two main corrections to ideal gas law must be introduced.

The first correction takes into account the quantum character of electrons, which obey the Pauli principle, and cannot occupy levels of energetic distribution which are already occupied by other electrons. This correction must be positive because it leads to an increased gas incompressibility.

Other correction takes into account the correlation of the screening action of charged particles inside dense plasma. It is the so-called correlational correction. Inside a dense plasma, the charged particles screen the fields of other charged particles. It leads to a decreasing of the pressure of charged particles. Accordingly, the correction for the correlation of charged particles must be negative, because it increases the compressibility of electron gas.

#### 2.1.2 The hot plasma energy with taking into account the correction for the Fermi-statistic

The energy of the electron gas in the Boltzmann's case ( $kT \gg \mathcal{E}_F$ ) can be calculated using the expression of the full energy of a non-relativistic Fermi-particle system [4]:

$$\mathcal{E} = \frac{2^{1/2}Vm_e^{3/2}}{\pi^2\hbar^3} \int_0^\infty \frac{\varepsilon^{3/2}d\varepsilon}{e^{(\varepsilon-\mu_e)/kT} + 1}, \quad (8)$$

expanding it in a series ( $m_e$  is electron mass,  $\varepsilon$  is the energy of electron and  $\mu_e$  is its chemical potential).

In the Boltzmann's case,  $\mu_e < 0$  and  $|\mu_e/kT| \gg 1$  and the integrand at

$e^{\mu_e/kT} \ll 1$  can be expanded into a series according to powers  $e^{\mu_e/kT - \varepsilon/kT}$ . If we introduce the notation  $z = \frac{\varepsilon}{kT}$  and conserve the two first terms of the series, we obtain

$$I \equiv (kT)^{5/2} \int_0^\infty \frac{z^{3/2} dz}{e^{z - \mu_e/kT} + 1} \approx \approx (kT)^{5/2} \int_0^\infty z^{3/2} \left( e^{\frac{\mu_e}{kT} - z} - e^{2(\frac{\mu_e}{kT} - z)} + \dots \right) dz \quad (9)$$

or

$$\frac{I}{(kT)^{5/2}} \approx e^{\frac{\mu_e}{kT}} \Gamma\left(\frac{3}{2} + 1\right) - \frac{1}{2^{5/2}} e^{\frac{2\mu_e}{kT}} \Gamma\left(\frac{3}{2} + 1\right) \approx \approx \frac{3\sqrt{\pi}}{4} e^{\mu_e/kT} \left( 1 - \frac{1}{2^{5/2}} e^{\mu_e/kT} \right). \quad (10)$$

Thus, the full energy of the hot electron gas is

$$\mathcal{E} \approx \frac{3V}{2} \frac{(kT)^{5/2}}{\sqrt{2}} \left( \frac{m_e}{\pi \hbar^2} \right)^{3/2} \left( e^{\mu_e/kT} - \frac{1}{2^{5/2}} e^{2\mu_e/kT} \right). \quad (11)$$

Using the definition of a chemical potential of ideal gas (of particles with spin=1/2) [4]

$$\mu_e = kT \log \left[ \frac{N_e}{2V} \left( \frac{2\pi \hbar^2}{m_e kT} \right)^{3/2} \right] \quad (12)$$

we obtain the full energy of the hot electron gas

$$\mathcal{E}_e \approx \frac{3}{2} kT N_e \left[ 1 + \frac{\pi^{3/2}}{4} \left( \frac{a_B e^2}{kT} \right)^{3/2} n_e \right], \quad (13)$$

where  $a_B = \frac{\hbar^2}{m_e e^2}$  is the Bohr radius.

### 2.1.3 The correction for correlation of charged particles in a hot plasma

At high temperatures, the plasma particles are uniformly distributed in space. At this limit, the energy of ion-electron interaction tends to zero. Some correlation in space distribution of particles arises as the positively charged particle groups around itself preferably particles with negative charges and vice versa. It is accepted to estimate the energy of this correlation by the method developed by Debye-Hückel for strong electrolytes [4]. The energy of a charged particle inside plasma is equal to  $e\varphi$ , where  $e$  is the charge of a particle, and  $\varphi$  is the electric potential induced by other particles on the considered particle.

This potential inside plasma is determined by the Debye law [4]:

$$\varphi(r) = \frac{e}{r} e^{-\frac{r}{r_D}} \quad (14)$$

where the Debye radius is

$$r_D = \left( \frac{4\pi e^2}{kT} \sum_a n_a Z_a^2 \right)^{-1/2} \quad (15)$$

For small values of ratio  $\frac{r}{r_D}$ , the potential can be expanded into a series

$$\varphi(r) = \frac{e}{r} - \frac{e}{r_D} + \dots \quad (16)$$

The following terms are converted into zero at  $r \rightarrow 0$ . The first term of this series is the potential of the considered particle. The second term

$$\mathcal{E} = -e^3 \sqrt{\frac{\pi}{kTV}} \left( \sum_a N_a Z_a^2 \right)^{3/2} \quad (17)$$

is a potential induced by other particles of plasma on the charge under consideration. And so the correlation energy of plasma consisting of  $N_e$  electrons and  $(N_e/Z)$  nuclei with charge  $Z$  in volume  $V$  is [4]

$$\mathcal{E}_{corr} = -e^3 \sqrt{\frac{\pi n_e}{kT}} Z^{3/2} N_e \quad (18)$$

## 2.2 The energy-preferable state of a hot plasma

### 2.2.1 The energy-preferable density of a hot plasma

Finally, under consideration of both main corrections taking into account the inter-particle interaction, the full energy of plasma is given by

$$\mathcal{E} \approx \frac{3}{2}kTN_e \left[ 1 + \frac{\pi^{3/2}}{4} \left( \frac{a_B e^2}{kT} \right)^{3/2} n_e - \frac{2\pi^{1/2}}{3} \left( \frac{Z}{kT} \right)^{3/2} e^3 n_e^{1/2} \right] \quad (19)$$

The plasma into a star has a feature. A star generates the energy into its inner region and radiates it from the surface. At the steady state of a star, its substance must be in the equilibrium state with a minimum of its energy. The radiation is not in equilibrium of course and can be considered as a star environment. The equilibrium state of a body in an environment is related to the minimum of the function ([4]§20):

$$\mathcal{E} - T_o S + P_o V, \quad (20)$$

where  $T_o$  and  $P_o$  are the temperature and the pressure of an environment. At taking into account that the star radiation is going away into vacuum, the two last items can be neglected and one can obtain the equilibrium equation of a star substance as the minimum of its full energy:

$$\frac{d\mathcal{E}_{plasma}}{dn_e} = 0. \quad (21)$$

Now taking into account Eq.(19), one obtains that an equilibrium condition corresponds to the equilibrium density of the electron gas of a hot plasma

$$n_e^{equilibrium} \equiv n_* = \frac{16}{9\pi} \frac{Z^3}{a_B^3} \approx 1.2 \cdot 10^{24} Z^3 cm^{-3}, \quad (22)$$

It gives the electron density  $\approx 3 \cdot 10^{25} cm^{-3}$  for the equilibrium state of the hot plasma of helium.

### 2.2.2 The estimation of temperature of energy-preferable state of a hot stellar plasma

As the steady-state value of the density of a hot non-relativistic plasma is known, we can obtain an energy-preferable temperature of a hot non-relativistic plasma.

The virial theorem [4],[5] claims that the full energy of particles  $E$ , if they form a stable system with the Coulomb law interaction, must be equal to their kinetic energy  $T$  with a negative sign. Neglecting small corrections at a high temperature, one can write the full energy of a hot dense plasma as

$$\mathcal{E}_{plasma} = U + \frac{3}{2}kTN_e = -\frac{3}{2}kTN_e. \quad (23)$$

Where  $U \approx -\frac{GM^2}{\mathbb{R}_0}$  is the potential energy of the system,  $G$  is the gravitational constant,  $M$  and  $\mathbb{R}_0$  are the mass and the radius of the star.

As the plasma temperature is high enough, the energy of the black radiation cannot be neglected. The full energy of the stellar plasma depending on the particle energy and the black radiation energy

$$\mathcal{E}_{total} = -\frac{3}{2}kTN_e + \frac{\pi^2}{15} \left( \frac{kT}{\hbar c} \right)^3 V kT \quad (24)$$

at equilibrium state must be minimal, i.e.

$$\left( \frac{\partial \mathcal{E}_{total}}{\partial T} \right)_{N,V} = 0. \quad (25)$$

This condition at  $\frac{N_e}{V} = n_*$  gives a possibility to estimate the temperature of the hot stellar plasma at the steady state:

$$T_* \approx Z \frac{\hbar c}{ka_B} \approx 10^7 Z K. \quad (26)$$

The last obtained estimation can raise doubts. At "terrestrial" conditions, the energy of any substance reduces to a minimum at  $T \rightarrow 0$ . It is caused by a positivity of a heat capacity of all of substances. But the steady-state energy of star is negative and its absolute value increases with increasing of temperature (Eq.(23)). It is the main property of a star as a thermodynamical object. This effect is a reflection of an influence of the gravitation on a stellar substance and is characterized by a negative effective heat capacity. The own heat capacity of a stellar substance (without gravitation) stays positive. With the increasing of the temperature, the role of the black radiation increases ( $\mathcal{E}_{br} \sim T^4$ ). When its role dominates, the star obtains a positive heat capacity. The energy minimum corresponds to a point between these two branches.

### 2.2.3 Are accepted assumptions correct?

At expansion in series of the full energy of a Fermi-gas, it was supposed that the condition of applicability of Boltzmann-statistics (5) is valid. The substitution of obtained values of the equilibrium density  $n_*$  (Eq.22) and equilibrium temperature  $\mathbb{T}_*$  (Eq.26) shows that the ratio

$$\frac{\mathcal{E}_F(n_*)}{k\mathbb{T}_*} \approx 3.1Z\alpha \ll 1. \quad (27)$$

Where  $\alpha \approx \frac{1}{137}$  is fine structure constant.

At appropriate substitution, the condition of expansion in series of the electric potential (Eq.16) gives

$$\frac{r}{r_D} \approx (n_*^{1/3} r_D)^{-1} \approx \alpha^{1/2} \ll 1. \quad (28)$$

Thus, obtained values of steady-state parameters of plasma are in full agreement with assumptions which was made above.

## 3 The gravity induced electric polarization in a dense hot plasma

### 3.1 Plasma cells

The existence of plasma at energetically favorable state with the constant density  $n_*$  and the constant temperature  $\mathbb{T}_*$  puts a question about equilibrium of this plasma in a gravity field. The Euler equation in commonly accepted form Eq.(1) disclaims a possibility to reach the equilibrium in a gravity field at a constant pressure in the substance: the gravity inevitably must induce a pressure gradient into gravitating matter. To solve this problem, it is necessary to consider the equilibrium of a dense plasma in an gravity field in detail. At zero approximation, at a very high temperature, plasma can be considered as a "jelly", where electrons and nuclei are "smeared" over a volume. At a lower temperature and a high density, when an interpartical interaction cannot be neglected, it is accepted to consider a plasma dividing in cells [6]. Nuclei are placed at centers of these cells, the rest of their volume is filled by electron gas. Its density decreases from the center of a cell to its periphery. Of course, this dividing is not freezed. Under action of heat processes, nuclei move. But having a small mass, electrons have time to trace this moving and to form a permanent electron cloud around nucleus, i.e. to form a cell. So plasma under action of a gravity must be characterized by two equilibrium conditions:

- the condition of an equilibrium of the heavy nucleus inside a plasma cell;
- the condition of an equilibrium of the electron gas, or equilibrium of cells.

### 3.2 The equilibrium of a nucleus inside plasma cell filled by an electron gas

At the absence of gravity, the negative charge of an electron cloud inside a cell exactly balances the positive charge of the nucleus at its center. Each cell is fully electroneutral. There is no direct interaction between nuclei.

The gravity acts on electrons and nuclei at the same time. Since the mass of nuclei is large, the gravity force applied to them is much larger than the force applied to electrons. On the another hand, as nuclei have no direct interaction, the elastic properties of plasma are depending on the electron gas reaction. Thus there is a situation, where the force applied to nuclei must be balanced by the force of the electron subsystem. The cell obtains an electric dipole moment  $d_s$ , and the plasma obtains polarization  $\mathfrak{P} = n_s d_s$ , where  $n_s$  is the density of the cell.

It is known [7], that the polarization of neighboring cells induces in the considered cell the electric field intensity

$$E_s = \frac{4\pi}{3} \mathfrak{P}, \quad (29)$$

and the cell obtains the energy

$$\mathcal{E}_s = \frac{d_s E_s}{2}. \quad (30)$$

The gravity force applied to the nucleus is proportional to its mass  $Am_p$  (where  $A$  is a mass number of the nucleus,  $m_p$  is the proton mass). The cell consists of  $Z$  electrons, the gravity force applied to the cell electron gas is proportional to  $Zm_e$  (where  $m_e$  is the electron mass). The difference of these forces tends to pull apart centers of positive and negative charges and to increase the dipole moment. The electric field  $E_s$  resists it. The process obtains equilibrium at the balance of the arising electric force  $\nabla \mathcal{E}_s$  and the difference of gravity forces applied to the electron gas and the nucleus:

$$\nabla \left( \frac{2\pi}{3} \frac{\mathfrak{P}^2}{n_s} \right) + (Am_p - Zm_e)\mathbf{g} = 0 \quad (31)$$

Taking into account, that  $\mathbf{g} = -\nabla\psi$ , we obtain

$$\frac{2\pi}{3} \frac{\mathfrak{P}^2}{n_s} = (Am_p - Zm_e)\psi. \quad (32)$$

Hence,

$$\mathfrak{P}^2 = \frac{3GM_r}{2\pi r} n_e \left( \frac{A}{Z} m_p - m_e \right), \quad (33)$$

where  $\psi$  is the potential of the gravitational field,  $n_s = \frac{n_e}{Z}$  is the density of cell (nuclei),  $n_e$  is the density of the electron gas,  $M_r$  is the mass of a star containing inside a sphere with radius  $r$ .

### 3.3 The equilibrium in plasma electron gas subsystem

Nonuniformly polarized matter can be represented by an electric charge distribution with density [7]

$$\tilde{\varrho} = \frac{\text{div} E_s}{4\pi} = \frac{\text{div} \mathfrak{P}}{3}. \quad (34)$$

The full electric charge of cells placed inside the sphere with radius  $r$

$$Q_r = 4\pi \int_0^r \tilde{\varrho} r^2 dr \quad (35)$$

determinants the electric field intensity applied to a cell placed on a distance  $r$  from center of a star

$$\tilde{\mathbf{E}} = \frac{Q_r}{r^2} \quad (36)$$

As a result, the action of a nonuniformly polarized environment can be described by the force  $\tilde{\varrho}\tilde{\mathbf{E}}$ . This force must be taken into account in the formulating of equilibrium equation. It leads to the following form of the Euler equation:

$$\gamma \mathbf{g} + \tilde{\varrho}\tilde{\mathbf{E}} + \nabla P = 0 \quad (37)$$

## 4 The internal structure of a star

It was shown above that the state with the constant density is energetically favorable for a plasma at a very high temperature. The plasma in the central region of a star can possess by this property. The calculation made below shows that the mass of central region of a star with the constant density - the star core - is equal to 1/2 of the full star mass. Its radius is approximately equal to 1/10 of radius of a star, i.e. the core with high density take approximately 1/1000 part of the full volume of a star. The other half of a stellar matter is distributed over the region placed above the core. It has a relatively small density and it could be called as a star atmosphere.

### 4.1 The plasma equilibrium in the star core

In this case, the equilibrium condition (Eq.(31)) for the energetically favorable state of plasma with the steady density  $n_s = \text{const}$  is achieved at

$$\mathfrak{P} = \sqrt{G}\gamma_* r, \quad (38)$$

Here the mass density is  $\gamma_* \approx \frac{A}{2} m_p n_*$ . The polarized state of the plasma can be described by a state with an electric charge at the density

$$\tilde{\varrho} = \frac{1}{3} \text{div} \mathfrak{P} = \sqrt{G}\gamma_*, \quad (39)$$

and the electric field applied to a cell is

$$\tilde{\mathbf{E}} = \frac{\mathbf{g}}{\sqrt{G}}. \quad (40)$$

As a result, the electric force applied to the cell will fully balance the gravity action

$$\gamma \mathbf{g} + \tilde{\varrho}\tilde{\mathbf{E}} = 0 \quad (41)$$

at the zero pressure gradient

$$\nabla P = 0. \quad (42)$$

### 4.2 The main parameters of a star core (in order of values)

At known density  $n_*$  of plasma into a core and its equilibrium temperature  $T_*$ , it is possible to estimate the mass  $M_*$  of a star core and its radius  $R_*$ . In accordance with the virial theorem<sup>4</sup>, the kinetic energy of particles composing the steady system must be approximately equal to its potential energy with opposite sign:

$$\frac{GM_*^2}{R_*} \approx kT_* N_*. \quad (43)$$

Where  $N_* = \frac{4\pi}{3} R_*^3 n_*$  is full number of particle into the star core.

With using determinations derived above (22) and (26) derived before, we obtain

$$M_* \approx \frac{M_{Ch}}{(A/Z)^2} \quad (44)$$

<sup>4</sup>Below we shall use this theorem in its more exact formulation.



where  $M_{Ch} = \left(\frac{\hbar c}{Gm_p^2}\right)^{3/2} m_p$  is the Chandrasekhar mass.

The radius of the core is approximately equal

$$R_* \approx \left(\frac{\hbar c}{Gm_p^2}\right)^{1/2} \frac{a_B}{Z(A/Z)}. \quad (45)$$

where  $A$  and  $Z$  are the mass and the charge number of atomic nuclei the plasma consisting of.

### 4.3 The equilibrium state of the plasma inside the star atmosphere

The star core is characterized by the constant mass density, the charge density, the temperature and the pressure. At a temperature typical for a star core, the plasma can be considered as ideal gas, as interactions between its particles are small in comparison with  $kT_*$ . In atmosphere, near surface of a star, the temperature is approximately by 3 ÷ 4 orders smaller. But the plasma density is lower. Accordingly, interparticle interaction is lower too and we can continue to consider this plasma as ideal gas.

In the absence of the gravitation, the equilibrium state of ideal gas in some volume comes with the pressure equalization, i.e. with the equalization of its temperature  $T$  and its density  $n$ . This equilibrium state is characterized by the equalization of the chemical potential of the gas  $\mu$  (Eq.(12)).

### 4.4 The radial dependence of density and temperature of substance inside a star atmosphere

For the equilibrium system, where different parts have different temperatures, the following relation of the chemical potential of particles to its temperature holds ([4],

25):

$$\frac{\mu}{kT} = const \quad (46)$$

As thermodynamic (statistical) part of chemical potential of monoatomic ideal gas is [4],45:

$$\mu_T = kT \ln \left[ \frac{n}{2} \left( \frac{2\pi\hbar^2}{mkT} \right)^{3/2} \right], \quad (47)$$

we can conclude that at the equilibrium

$$n \sim T^{3/2}. \quad (48)$$

In external fields the chemical potential of a gas [4]25 is equal to

$$\mu = \mu_T + \mathcal{E}^{potential} \quad (49)$$

where  $\mathcal{E}^{potential}$  is the potential energy of particles in the external field. Therefore in addition to fulfillment of condition Eq. (48), in a field with Coulomb potential, the equilibrium needs a fulfillment of the condition

$$-\frac{GM_r\gamma}{rkT_r} + \frac{\mathfrak{P}_r^2}{2kT_r} = const \quad (50)$$

(where  $m$  is the particle mass,  $M_r$  is the mass of a star inside a sphere with radius  $r$ ,  $\mathfrak{P}_r$  and  $T_r$  are the polarization and the temperature on its surface. As on the core surface, the left part of Eq.(50) vanishes, in the atmosphere

$$M_r \sim rkT_r. \quad (51)$$

Supposing that a decreasing of temperature inside the atmosphere is a power function with the exponent  $x$ , its value on a radius  $r$  can be written as

$$T_r = T_* \left( \frac{R_*}{r} \right)^x \quad (52)$$

and in accordance with Eq.(48), the density

$$n_r = n_* \left( \frac{R_*}{r} \right)^{3x/2}. \quad (53)$$

Setting the powers of  $r$  in the right and the left parts of the condition Eq.(51) equal, one can obtain  $x = 4$ .

Thus, at using power dependencies for the description of radial dependencies of density and temperature, we obtain

$$n_r = n_* \left( \frac{R_*}{r} \right)^6 \quad (54)$$

and

$$T_r = T_* \left( \frac{R_*}{r} \right)^4. \quad (55)$$

## 4.5 The mass of the star atmosphere and the full mass of a star

After integration of Eq.(54), we can obtain the mass of the star atmosphere

$$\begin{aligned} M_A &= 4\pi \int_{\mathbb{R}_*}^{\mathbb{R}_0} (A/Z)m_p n_* \left(\frac{\mathbb{R}_*}{r}\right)^6 r^2 dr = \\ &= \frac{4\pi}{3} (A/Z)m_p n_* \mathbb{R}_*^3 \left[1 - \left(\frac{\mathbb{R}_*}{\mathbb{R}_0}\right)^3\right] \end{aligned} \quad (56)$$

It is equal to its core mass

(to  $\frac{\mathbb{R}_*}{\mathbb{R}_0} \approx 10^{-3}$ ), where  $\mathbb{R}_0$  is radius of a star.

Thus, the full mass of a star

$$M = M_A + M_* \approx 2M_* \quad (57)$$

## 5 The virial theorem and main parameters of a star

### 5.1 The energy of a star

The virial theorem [4],[5] is applicable to a system of particles if they have a finite moving into a volume  $V$ . If their interaction obeys to the Coulomb's law, their potential energy  $\mathcal{E}^{potential}$ , their kinetic energy  $\mathcal{E}^{kinetic}$  and pressure  $P$  are in the ratio:

$$2\mathcal{E}^{kinetic} + \mathcal{E}^{potential} = 3PV. \quad (58)$$

On the star surface, the pressure is absent and for the particle system as a whole:

$$2\mathcal{E}^{kinetic} = -\mathcal{E}^{potential} \quad (59)$$

and the full energy of plasma particles into a star

$$\mathcal{E}(plasma) = \mathcal{E}^{kinetic} + \mathcal{E}^{potential} = -\mathcal{E}^{kinetic}. \quad (60)$$

Let us calculate the separate items composing the full energy of a star.

### 5.2 The kinetic energy of plasma

The kinetic energy of plasma into a core:

$$\mathcal{E}_*^{kinetic} = \frac{3}{2} k T_* N_* \quad (61)$$

The kinetic energy of atmosphere:

$$\mathcal{E}_a^{kinetic} = 4\pi \int_{\mathbb{R}_*}^{\mathbb{R}_0} \frac{3}{2} k T_* n_* \left(\frac{\mathbb{R}_*}{r}\right)^{10} r^2 dr \approx \frac{3}{7} \left(\frac{3}{2} k T_* N_*\right) \quad (62)$$

The total kinetic energy of plasma particles

$$\mathcal{E}^{kinetic} = \mathcal{E}_*^{kinetic} + \mathcal{E}_a^{kinetic} = \frac{15}{7} k T_* N_* \quad (63)$$

### 5.3 The potential energy of star plasma

Inside a star core, the gravity force is balanced by the force of electric nature. Correspondingly, the energy of electric polarization can be considered as balanced by the gravitational energy of plasma. As a result, the potential energy of a core can be considered as equal to zero.

In a star atmosphere, this balance is absent.

The gravitational energy of an atmosphere

$$\mathcal{E}_a^G = -4\pi G M_* \frac{A}{Z} m_p n_* \int_{\mathbb{R}_*}^{\mathbb{R}_0} \frac{1}{2} \left[2 - \left(\frac{\mathbb{R}_*}{r}\right)^3\right] \left(\frac{\mathbb{R}_*}{r}\right)^6 r dr \quad (64)$$

or

$$\mathcal{E}_a^G = \frac{3}{2} \left(\frac{1}{7} - \frac{1}{2}\right) \frac{G M_*^2}{\mathbb{R}_*} = -\frac{15}{28} \frac{G M_*^2}{\mathbb{R}_*} \quad (65)$$

The electric energy of atmosphere is

$$\mathcal{E}_a^E = -4\pi \int_{\mathbb{R}_*}^{\mathbb{R}_0} \frac{1}{2} \rho \varphi r^2 dr, \quad (66)$$

where

$$\tilde{\varrho} = \frac{1}{3r^2} \frac{d\mathfrak{P}r^2}{dr} \quad (67)$$

and

$$\tilde{\varphi} = \frac{4\pi}{3} \mathfrak{P}r. \quad (68)$$

The electric energy:

$$\mathcal{E}_a^E = -\frac{3}{28} \frac{GM_\star^2}{\mathbb{R}_\star}, \quad (69)$$

and total potential energy of atmosphere:

$$\mathcal{E}_a^{potential} = \mathcal{E}_a^G + \mathcal{E}_a^E = -\frac{9}{14} \frac{GM_\star^2}{\mathbb{R}_\star}. \quad (70)$$

The equilibrium in a star depends both on plasma energy and energy of radiation.

## 5.4 The temperature of a star core

### 5.4.1 The energy of the black radiation

The energy of black radiation inside a star core is

$$\mathcal{E}_\star(br) = \frac{\pi^2}{15} kT_\star \left( \frac{kT_\star}{\hbar c} \right)^3 V_\star. \quad (71)$$

The energy of black radiation inside a star atmosphere is

$$\begin{aligned} \mathcal{E}_a(br) &= \\ &= 4\pi \int_{R_\star}^{R_0} \frac{\pi^2}{15} kT_\star \left( \frac{kT_\star}{\hbar c} \right)^3 \left( \frac{\mathbb{R}_\star}{r} \right)^{16} r^2 dr = \\ &= \frac{3}{13} \frac{\pi^2}{15} kT_\star \left( \frac{kT_\star}{\hbar c} \right)^3 V_\star. \end{aligned} \quad (72)$$

The total energy of black radiation inside a star is

$$\begin{aligned} \mathcal{E}(br) &= \mathcal{E}_\star(br) + \mathcal{E}_a(br) = \\ &= \frac{16}{13} \frac{\pi^2}{15} kT_\star \left( \frac{kT_\star}{\hbar c} \right)^3 V_\star = 1.23 \frac{\pi^2}{15} kT_\star \left( \frac{kT_\star}{\hbar c} \right)^3 V_\star \end{aligned} \quad (73)$$

### 5.4.2 The full energy of a star

In accordance with (60), the full energy of a star

$$\mathcal{E}^{star} = -\mathcal{E}^{kinetic} + \mathcal{E}(br) \quad (74)$$

i.e.

$$\mathcal{E}^{star} = -\frac{15}{7} kT_\star N_\star + \frac{16}{13} \frac{\pi^2}{15} kT_\star \left( \frac{kT_\star}{\hbar c} \right)^3 V_\star. \quad (75)$$

The steady state of a star is determined by a minimum of its full energy:

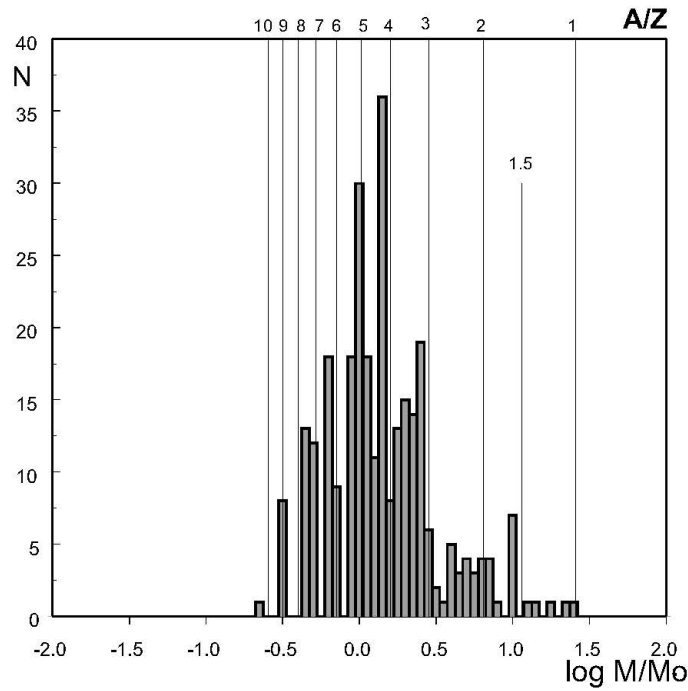
$$\left( \frac{d\mathcal{E}^{star}}{dT_\star} \right)_{N=const, V=const} = 0, \quad (76)$$

it corresponds to the condition:

$$-\frac{15}{7} N_\star + \frac{64\pi^2}{13 \cdot 15} \left( \frac{kT_\star}{\hbar c} \right)^3 V_\star = 0. \quad (77)$$

Together with Eq.(22) it defines the equilibrium temperature of a star core:

$$T_\star = \left( \frac{25 \cdot 13}{28\pi^4} \right)^{1/3} \left( \frac{\hbar c}{ka_B} \right) Z \approx Z \cdot 2.13 \cdot 10^7 K \quad (78)$$



**Figure 1.** The mass distribution of binary stars [8]. On abscissa, the logarithm of the star mass over the Sun mass is shown. Solid lines mark masses, which agree with selected values of  $A/Z$  from Eq.(83).

## 5.5 Main star parameters

### 5.5.1 The star mass

The virial theorem connect kinetic energy of a system with its potential energy. In accordance with Eqs.(70) and (63)

$$\frac{9}{14} \frac{GM_{\star}^2}{R_{\star}} = \frac{30}{7} kT_{\star} N_{\star}. \quad (79)$$

Introducing the non-dimensional parameter

$$\eta = \frac{GM_{\star} \frac{A}{Z} m_p}{R_{\star} kT_{\star}}, \quad (80)$$

we obtain

$$\eta = \frac{20}{3} = 6.67, \quad (81)$$

and at taking into account Eqs.(22) and (78), the core mass is

$$M_{\star} = \left[ \frac{20}{3} \left( \frac{25 \cdot 13}{28} \right)^{1/3} \frac{3}{4 \cdot 3.14} \right]^{3/2} \frac{M_{Ch}}{\left( \frac{A}{Z} \right)^2} = 6.84 \frac{M_{Ch}}{\left( \frac{A}{Z} \right)^2} \quad (82)$$

The obtained equation plays a very important role, because together with Eq.(57), it gives a possibility to predict the total mass of a star:

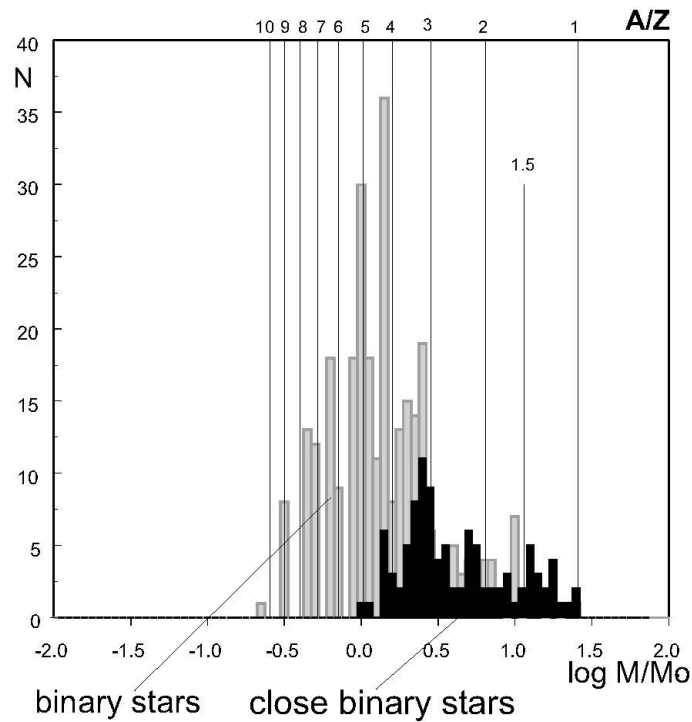
$$M = 2M_{\star} = \frac{13.68 M_{Ch}}{\left( \frac{A}{Z} \right)^2} \approx \frac{25.34 M_{\odot}}{\left( \frac{A}{Z} \right)^2}. \quad (83)$$

The comparison of obtained prediction Eq.(83) with measuring data gives a method to check our theory. Although there is no way to determine chemical composition of cores of far stars, some predictions can be made in this way. At first, there must be no stars which masses exceed the mass of the Sun by more than one and a half orders, because it accords to limiting mass of stars consisting from hydrogen with  $A/Z = 1$ . Secondly, the action of a specific mechanism (see Part III, Sec.1) can make neutron-excess nuclei stable, but it don't give a base to suppose that stars with  $A/Z > 10$  (and with mass in hundred times less than hydrogen stars) can exist. Thus, the theory predicts that the whole mass spectrum must be placed in the interval from 0.25 up to approximately 25 solar masses. These predication are verified by measurements quite exactly. The mass distribution of binary stars<sup>5</sup> is shown in Fig.1 [8].

The mass spectrum of close binary stars<sup>6</sup> is shown in Fig.2.

<sup>5</sup>The using of these data is caused by the fact that only the measurement of parameters of binary star rotation gives a possibility to determine their masses with satisfactory accuracy.

<sup>6</sup>The data of these measurements were obtained in different observatories of the world. The last time the summary table with these data was gathered by Khaliulilin Kh.F. (Sternberg Astronomical Institute) [9] in his dissertation (in Russian) which has unfortunately has a restricted access. With his consent and for readers convenience, we place that table in Appendix.



**Figure 2.** The mass distribution of close binary stars [9]. On abscissa, the logarithm of the star mass over the Sun mass is shown. Solid lines mark masses, which agree with selected values of  $A/Z$  from Eq.(83). The binary star spectrum is shown for comparison.

The very important element of the direct and clear confirmation of the theory is obviously visible on these figures - both spectra is dropped near the value  $A/Z = 1$ .

Beside it, one can easily see that the mass spectrum of binary stars (Fig.(1)) consists of series of well-isolated lines which are representing the stars with integer values of ratios  $A/Z = 3, 4, 5, \dots$ , corresponding hydrogen-3,4,5 ... or helium-6,8,10 ... (also line with the half-integer ratio  $A/Z = 3/2$ , corresponding, probably, to helium-3, Be-6, C-9...). The existence of stable stars with ratios  $A/Z \geq 3$  raises questions. It is generally assumed that stars are composed of hydrogen-1, deuterium, helium-4 and other heavier elements with  $A/Z \approx 2$ . Nuclei with  $A/Z \geq 3$  are the neutron-excess and so short-lived, that they can not build a long-lived stars. Neutron-excess nuclei can become stable under the action of mechanism of neutronization, which is acting inside the dwarfs. It is accepted to think that this mechanism must not work into the stars. The consideration of the effecting of the electron gas of a dense plasma on the nucleus is described in Part III, Sec.1. These calculations show that the electron gas of dense plasma should also lead to the neutronization mechanism and to the stabilization of the neutron-excess nuclei. This explains the existence of a stable of stars, where the plasma consists of nuclei with  $A/Z \geq 3$ .

Beside it, at considering of Fig.(1), the question is arising: why there are so few stars, which are composed by very stable nuclei of helium-4? At the same time, there are many stars with  $A/Z = 4$ , i.e. consisting apparently of a hydrogen-4, as well as stars with  $A/Z = 3/2$ , which hypothetically could be composed by another isotope of helium - helium-3. This equation is discussed in Part III, Sec.1.

It is important to note, that according to Eq.(83) the Sun must consist from a substance with  $A/Z = 5$ . This conclusion is in a good agreement with results of consideration of solar oscillations (Part II).

### 5.5.2 Radii of stars

Using Eq.(22) and Eq.(82), we can determine the star core radius:

$$R_* = 1.42 \frac{a_B}{Z(A/Z)} \left( \frac{\hbar c}{G m_p^2} \right)^{1/2} \approx \frac{9.79 \cdot 10^{10}}{Z(A/Z)} \text{ cm.} \quad (84)$$

The temperature near the star surface is relatively small. It is approximately by 3 orders smaller than it is inside the core. Because of it at calculation of surface parameters, we must take into consideration effects of this order, i.e. it is necessary to take into account the gravity action on the electron gas. At that it is convenient to consider the plasma cell as some neutral quasi-atom (like the Thomas-Fermi atom). Its electron shell is formed by a cloud of free electrons.

Each such quasi-atom is retained on the star surface by its negative potential energy

$$(\mathcal{E}_{gravitational} + \mathcal{E}_{electric}) < 0. \quad (85)$$

The electron cloud of the cell is placed in the volume  $\delta V = \frac{4\pi}{3} r_s^3$ , (where  $r_s \approx \left( \frac{Z}{n_e} \right)^{1/3}$ ) under pressure  $P_e$ . The evaporation of plasma cell releases energy  $\mathcal{E}_{PV} = P_e V_s$ , and the balance equation takes the form:

$$\mathcal{E}_{gravitational} + \mathcal{E}_{electric} + \mathcal{E}_{PV} = 0. \quad (86)$$

In cold plasma, the electron cloud of the cell has energy  $\mathcal{E}_{PV} \approx e^2 n_e^{1/3}$ . in very hot plasma at  $kT \gg \frac{Z^2 e^2}{r_s}$ , this energy is equal to  $\mathcal{E}_{PV} = \frac{3}{2} Z kT$ . On the star surface these energies are approximately equal:

$$\frac{kT_0}{e^2 n_e^{1/3}} \approx \frac{1}{\alpha} \left( \frac{\mathbb{R}_0}{\mathbb{R}_*} \right)^2 \approx 1. \quad (87)$$

One can show it easily, that in this case

$$\mathcal{E}_{PV} \approx 2Z \sqrt{\frac{3}{2} kT \cdot e^2 n_e^{1/3}}. \quad (88)$$

And if to take into account Eqs.(54)-(55), we obtain

$$\mathcal{E}_{PV} \approx 1.5 Z k T_* \left( \frac{\mathbb{R}_*}{\mathbb{R}_0} \right)^3 \sqrt{\alpha \pi} \quad (89)$$

The energy of interaction of a nucleus with its electron cloud does not change at evaporation of the cell and it can be neglected. Thus, for the surface

$$\mathcal{E}_{electric} = \frac{2\pi \mathfrak{P}^2}{3n_s} = \frac{2GM_*}{\mathbb{R}_0} (Am_p - Zm_e). \quad (90)$$

The gravitational energy of the cell on the surface

$$\mathcal{E}_{gravitational} = -\frac{2GM_*}{\mathbb{R}_0} (Am_p + Zm_e). \quad (91)$$

Thus, the balance condition Eq.(86) on the star surface obtains the form

$$-\frac{4GM_* Z m_e}{\mathbb{R}_0} + 1.5 Z k T_* \left( \frac{\mathbb{R}_*}{\mathbb{R}_0} \right)^3 \sqrt{\alpha \pi} = 0. \quad (92)$$

### 5.5.3 The $\mathbb{R}_*/\mathbb{R}_0$ ratio and $\mathbb{R}_0$

With account of Eq.(55) and Eqs.(81)-(80), we can write

$$\frac{\mathbb{R}_0}{\mathbb{R}_*} = \left( \frac{\sqrt{\alpha \pi} \frac{A}{Z} m_p}{2\eta m_e} \right)^{1/2} \approx 4.56 \sqrt{\frac{A}{Z}} \quad (93)$$

As the star core radius is known Eq.(84), we can obtain the star surface radius:

$$\mathbb{R}_0 \approx \frac{4.46 \cdot 10^{11}}{Z(A/Z)^{1/2}} cm. \quad (94)$$

### 5.5.4 The temperature of a star surface

At known Eq.(55) and Eq.(78), we can calculate the temperature of external surface of a star

$$T_0 = T_* \left( \frac{\mathbb{R}_*}{\mathbb{R}_0} \right)^4 \approx 4.92 \cdot 10^5 \frac{Z}{(A/Z)^2} \quad (95)$$

### 5.5.5 The comparison with measuring data

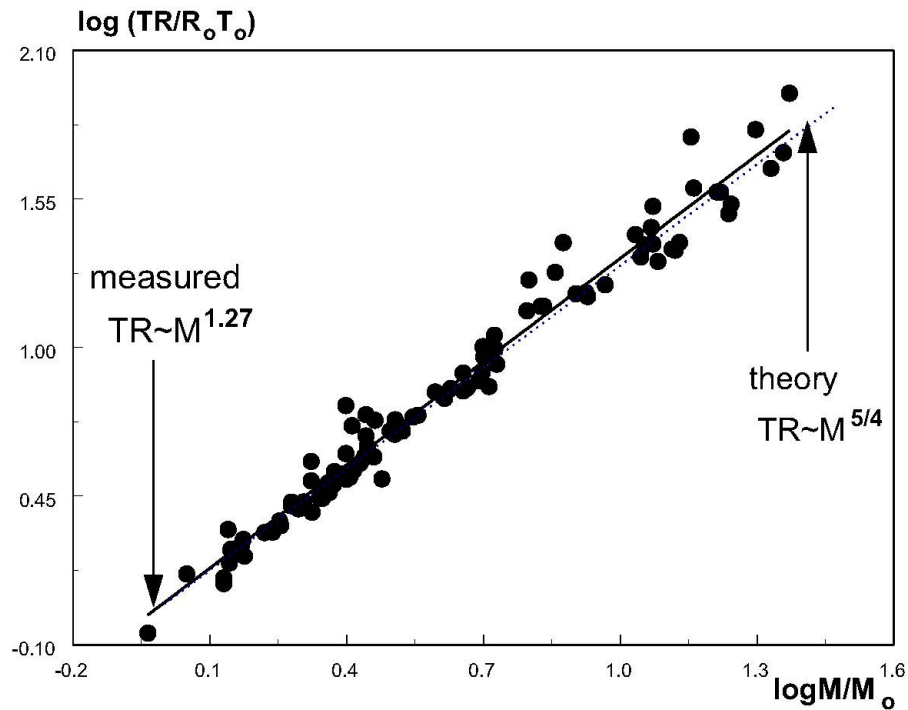
The mass spectrum (Fig.1) shows that the Sun consists basically from plasma with  $A/Z = 5$ . The radius of the Sun and its surface temperature are functions of  $Z$  too. This values calculated at  $A/Z=5$  and differen  $Z$  are shown in Table (1)

**Table 1.** The calculated stellar parameters

Z	$\mathbb{R}_\odot, cm$ (calculated (94))	$T_\odot, K$ (calculated (95))
1	$2.0 \cdot 10^{11}$	1961
2	$1.0 \cdot 10^{11}$	3923
3	$6.65 \cdot 10^{10}$	5885
4	$5.0 \cdot 10^{10}$	7845

One can see that these calculated data have a satisfactory agreement the measured radius of the Sun

$$\mathbb{R}_\odot = 6.96 \cdot 10^{10} cm \quad (96)$$



**Figure 3.** The relation between main parameters of stars (Eq.(103)) and corresponding data of astronomical measurements for close binary stars [9] are shown.

and the measured surface temperature

$$T_{\odot} = 5850 \text{ K} \quad (97)$$

at  $Z = 3$ .

The calculation shows that the mass of core of the Sun

$$M_{*}(Z = 3, A/Z = 5) \approx 9.68 \cdot 10^{32} \text{ g} \quad (98)$$

i.t. almost exactly equals to one half of full mass of the Sun

$$\frac{M_{*}(Z = 3, A/Z = 5)}{M_{\odot}} \approx 0.486 \quad (99)$$

in full agreement with Eq.(57).

In addition to obtained determinations of the mass of a star Eq.(83), its temperature Eq.(95) and its radius Eq.(94) give possibility to check the calculation, if we compare these results with measuring data. Really, dependencies measured by astronomers can be described by functions:

$$M = \frac{Const_1}{(A/Z)^2}, \quad (100)$$

$$R_0 = \frac{Const_2}{Z(A/Z)^{1/2}}, \quad (101)$$

$$T_0 = \frac{Const_3 Z}{(A/Z)^2}. \quad (102)$$

If to combine they in the way, to exclude unknown parameter  $Z$ , one can obtain relation:

$$T_0 R_0 = Const M^{5/4}, \quad (103)$$

Its accuracy can be checked. For this checking, let us use the measuring data of parameters of masses, temperatures and radii of close binary stars [9]. The results of these measurements are shown in Fig.(3), where the dependence according to Eq.(103). It is not difficult to see that these data are well described by the calculated dependence. It speaks about successfulness of our consideration.

If main parameters of the star are expressed through corresponding solar values  $\tau \equiv \frac{T_0}{T_{\odot}}$ ,  $\rho \equiv \frac{R_0}{R_{\odot}}$  and  $\mu \equiv \frac{M}{M_{\odot}}$ , that Eq.(103) can be rewritten as

$$\frac{\tau \rho}{\mu^{5/4}} = 1. \quad (104)$$

Numerical values of relations  $\frac{\tau\rho}{\mu^{5/4}}$  for close binary stars [9] are shown in the last column of tables Part II Sec.1.

---

## REFERENCES

- [1] Vasiliev B.V.: The gravity-induced electric polarization of electron-nuclear plasma and related astrophysical effects *Nuovo Cimento B*, **116**, pp.617-634, (2001)
- [2] Vasiliev B.V.: Why spontaneous electric polarization can arise inside cosmic bodies? *Nuovo Cimento B*, **112**, pp.1361-1372, (1997)
- [3] Vasiliev B.V.: Can the existence of the magnetic moments of cosmic bodies be explained by internal spontaneous electric polarization? *Nuovo Cimento B*, **110**, pp.381389, (1996)
- [4] Landau L.D. and Lifshits E.M.: *Statistical Physics*, **1**, 3rd edition, Oxford:Pergamon, (1980)
- [5] Vasiliev B.V. and Luboshits V.L.: *Physics-Uspeski*, **37**, 345, (1994)
- [6] Leung Y.C.: *Physics of Dense Matter* In Science Press/World Scientific, Beijing and Singapore, (1984)
- [7] Landau L.D. and Lifshits E.M.: *Electrodynamics of condensed matter*, **1**, 3rd edition, Oxford:Pergamon, (1980)
- [8] Heintz W.D.: *Double stars* In Geoph. and Astroph. monographs, **15**, D.Reidel Publ. Corp., (1978)
- [9] Khaliullin K.F.: *Dissertation*, Sternberg Astronomical Institute, Moscow, (Russian)(2004) (see Table in Part III-Appendix)